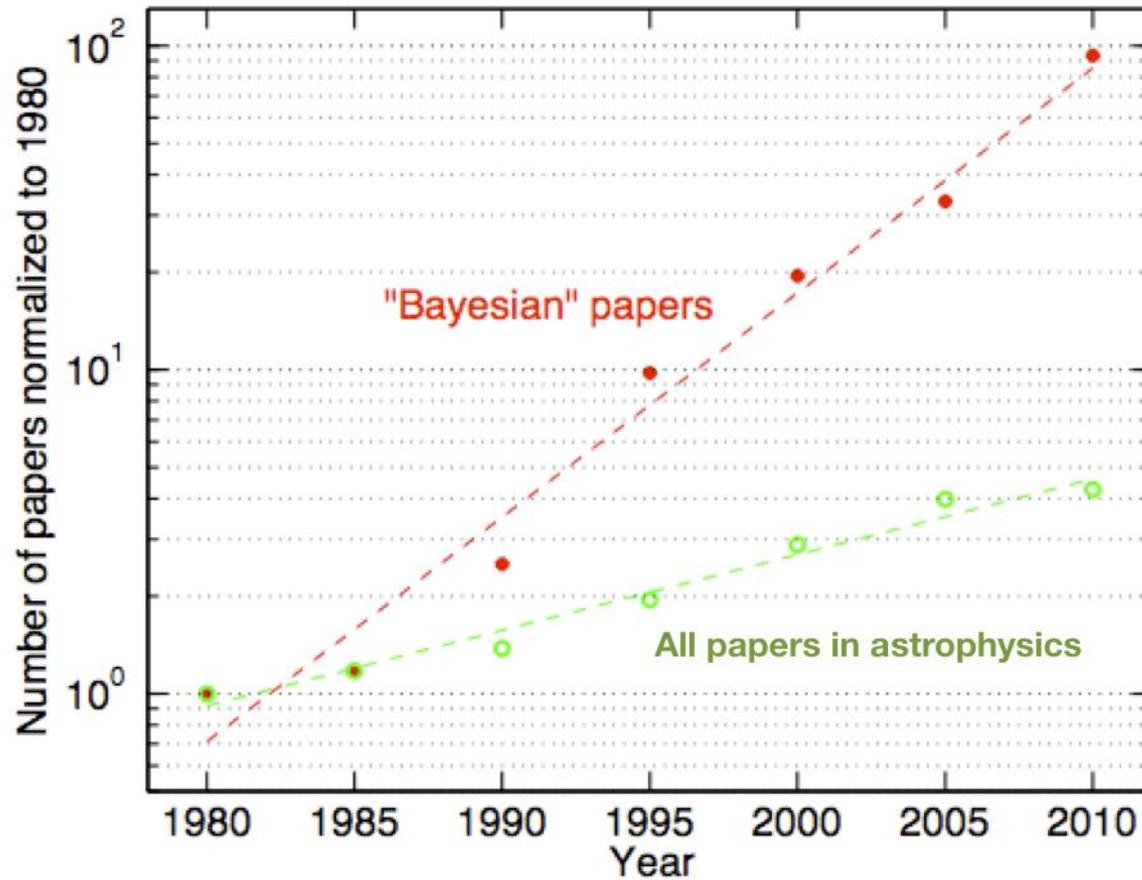
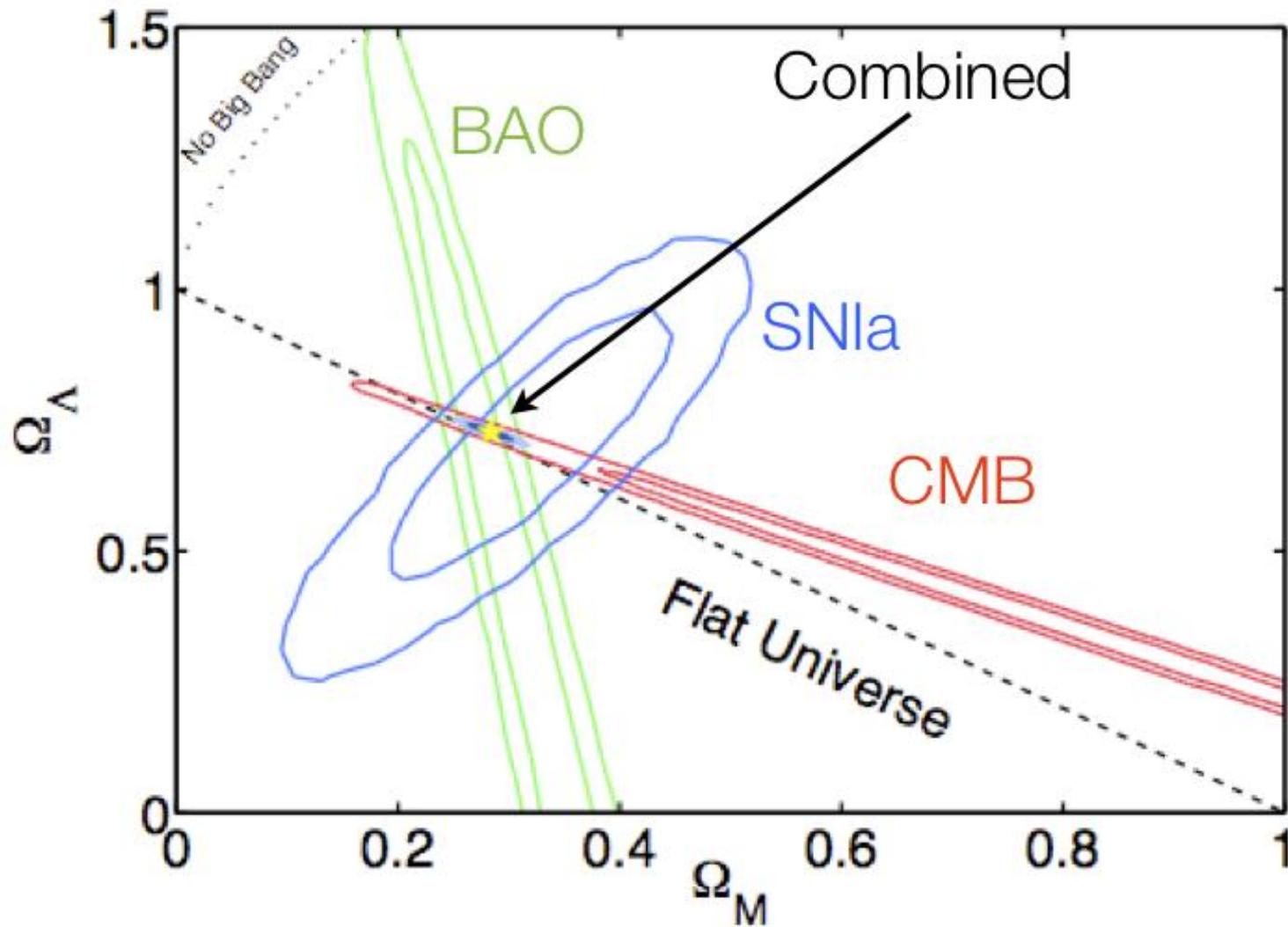


Astrostatistics

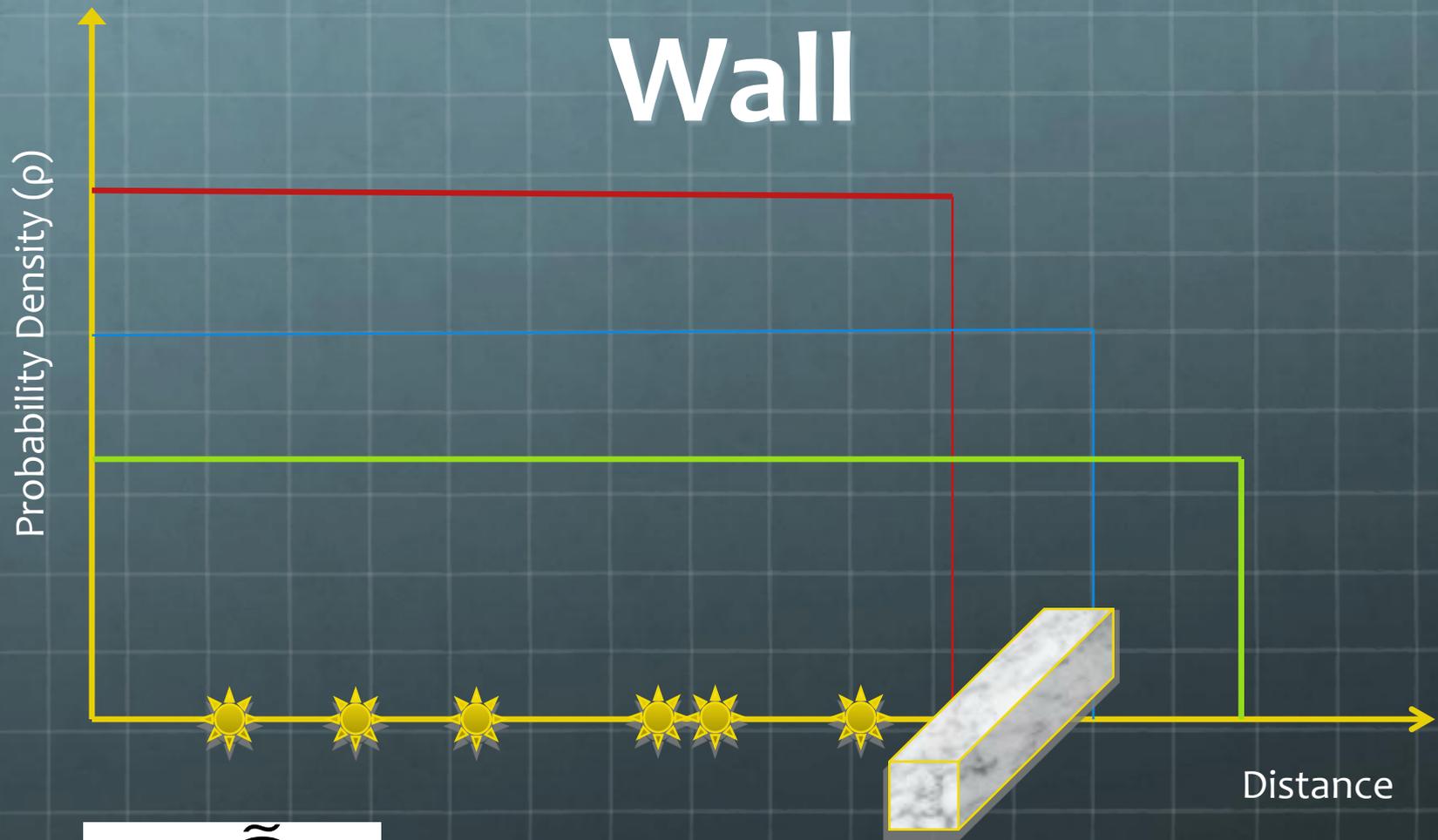
Tim Naylor – Head of Physics
Norman Lockyer Professor of Astrophysics

The rise of Bayesian methods in astrophysics





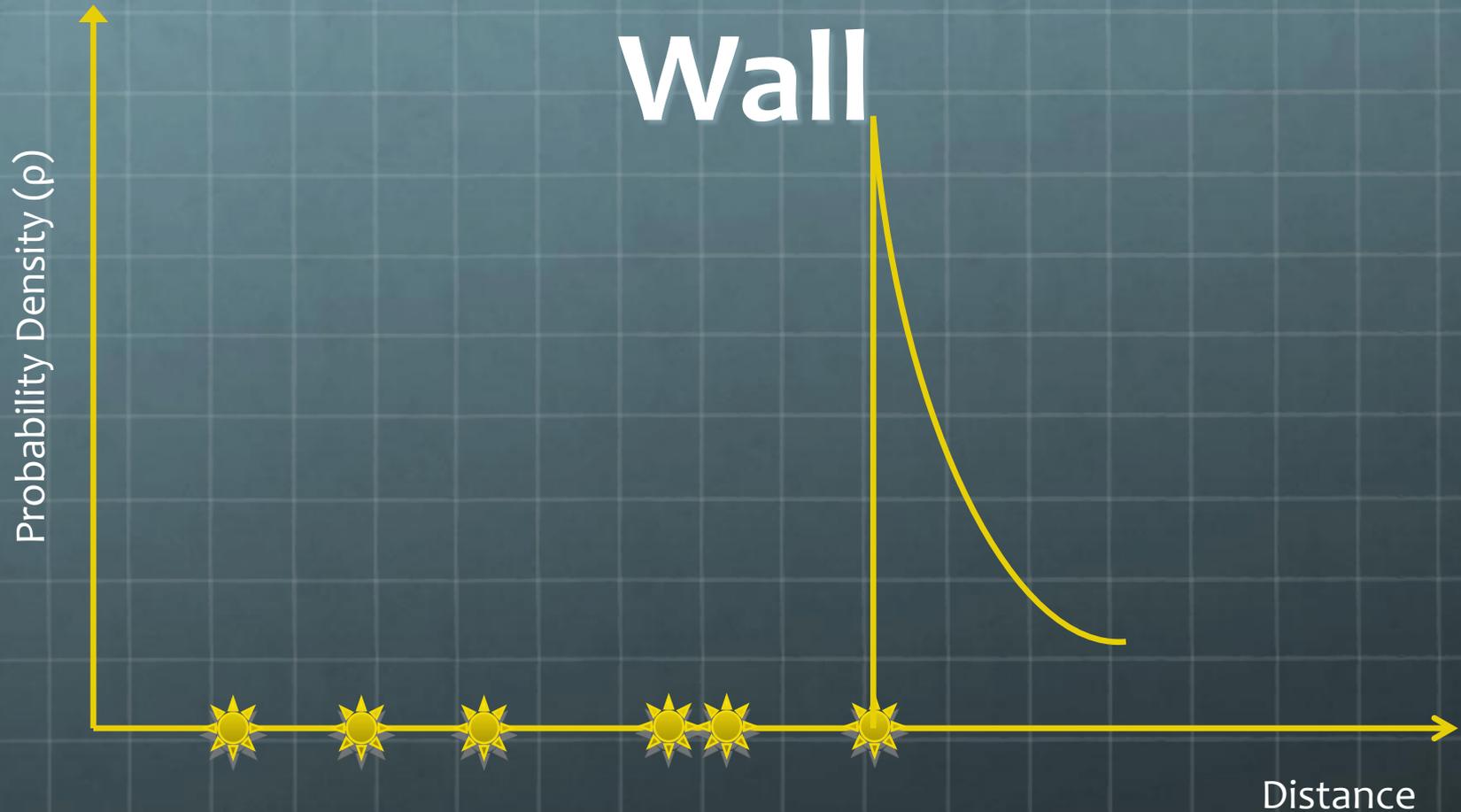
The Wildebeest and the Wall



$$\mathcal{L} = \tilde{\mathcal{O}} r_i$$

$i=1, N$

The Wildebeest and the Wall

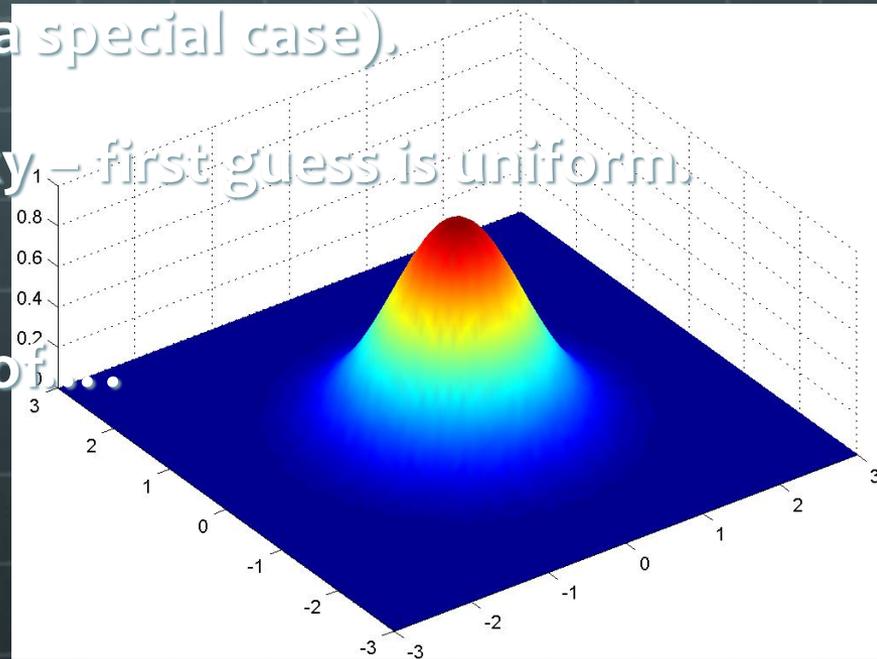


$$\mathcal{L} = \tilde{O} \sum_{i=1, N} r_i$$

$$t^2 = -2\tilde{a} \ln \int_0^{\infty} U_i(x - x_i) r(x) dx$$

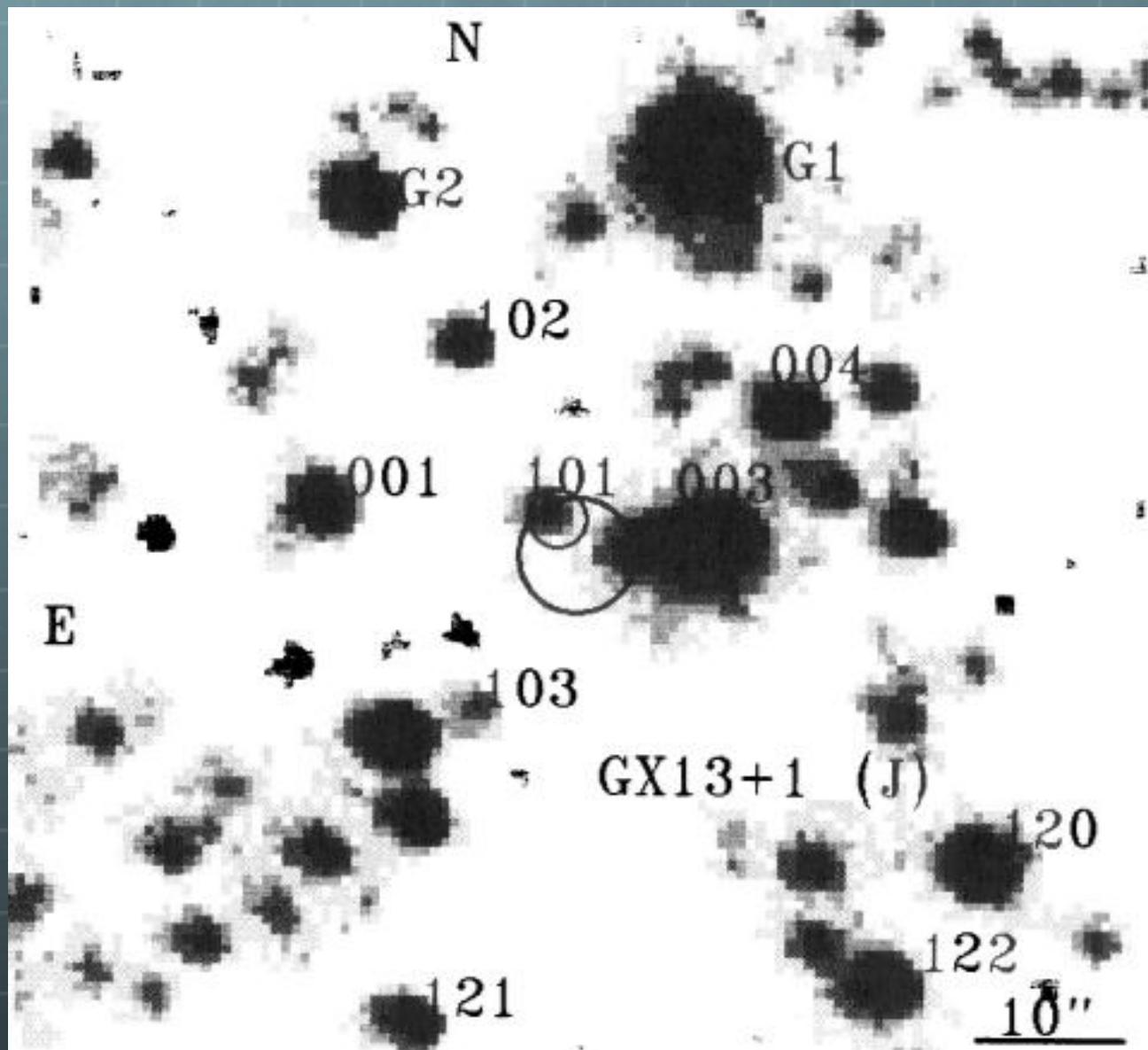
Uses

- 🌐 Problems where you might have used cumulative distributions (e.g. Kolmogorov-Smirnov tests).
- 🌐 Works well in higher dimensions.
- 🌐 Deals with error bars (χ^2 is a special case).
- 🌐 Positions of stars on the sky – first guess is uniform.
- 🌐 Add an extra star whose position you are uncertain of...



A Catalogue Matching Problem

- 🌍 You can test whether there is an “extra” star.
- 🌍 For any single star the ratio of the uniform model to the Gaussian at that point tells you the probability it is THE counterpart.
- 🌍 Two lists of sky co-ordinates for objects, one with large positional uncertainties – which objects should be paired together?



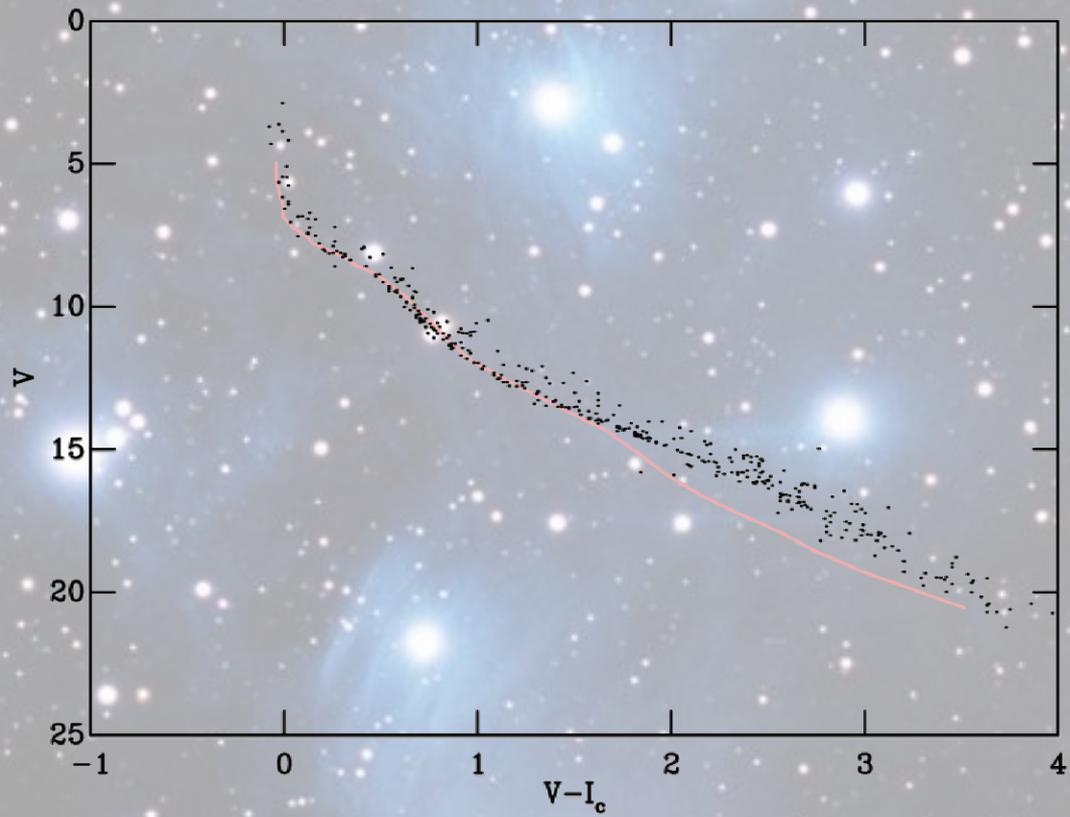
Naylor, Charles & Longmore (1991).

The Catalogue Matching Problem

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- 🌍 For any single star the ratio of the uniform model to the Gaussian at that point tells you the probability it is THE counterpart.
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- 🌍 In general you cannot catalogue match without some prejudice about expected properties.

Colour-Magnitude Diagrams

-  The simplest measurement of a star is its flux integrated over a given wavelength range (the log of which is its magnitude).
-  Next is the ratio between flux in one band and another (the log of which is its colour).
-  Pick a group of stars at the same distance and of the same age and you get a colour-magnitude diagram.

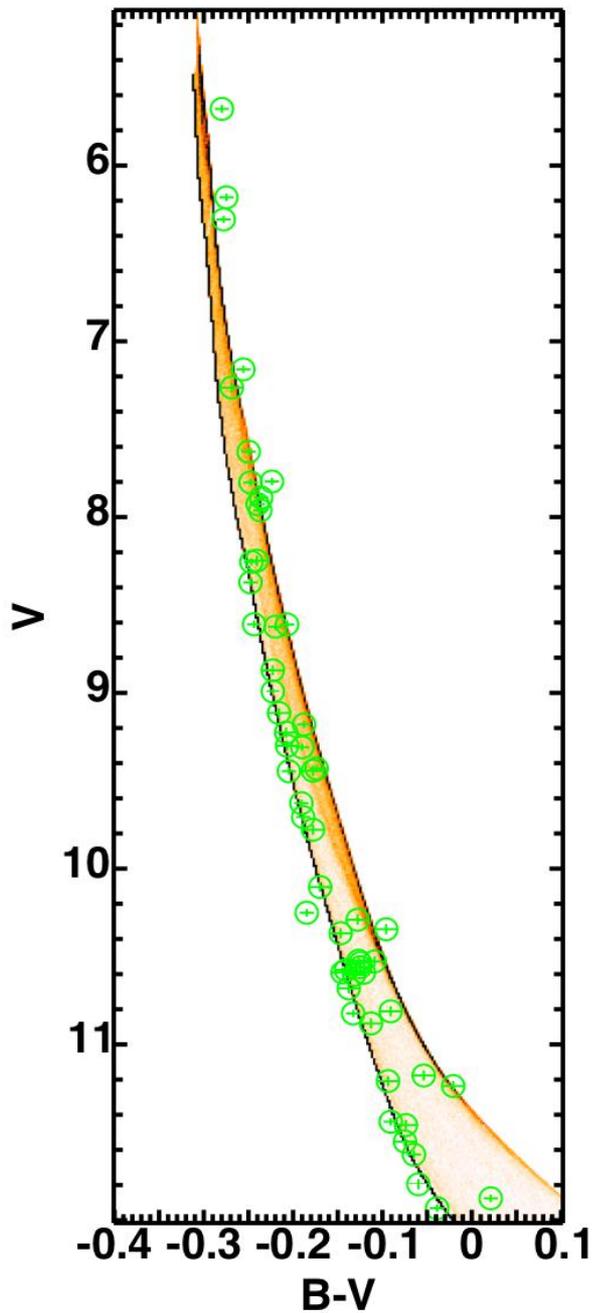


Nuclear Ages

NGC 6530

0.25 Myr (Geneva-Bessell)

$\text{Pr}(\tau^2)=0.03$

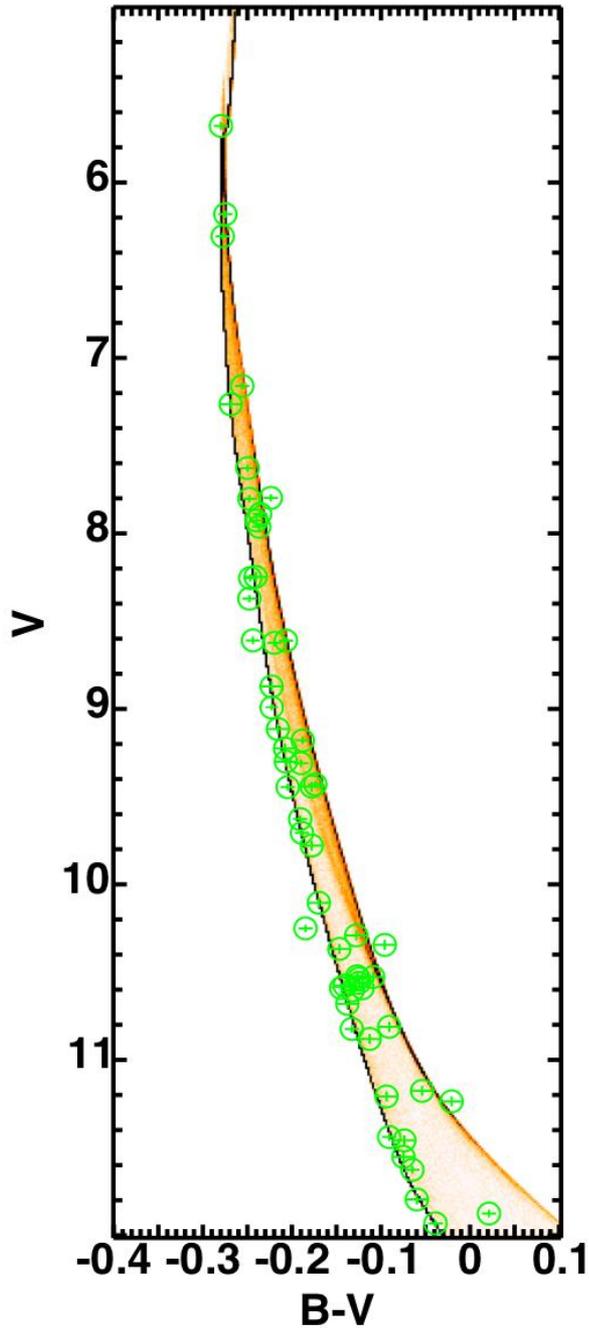


Nuclear Ages

NGC 6530

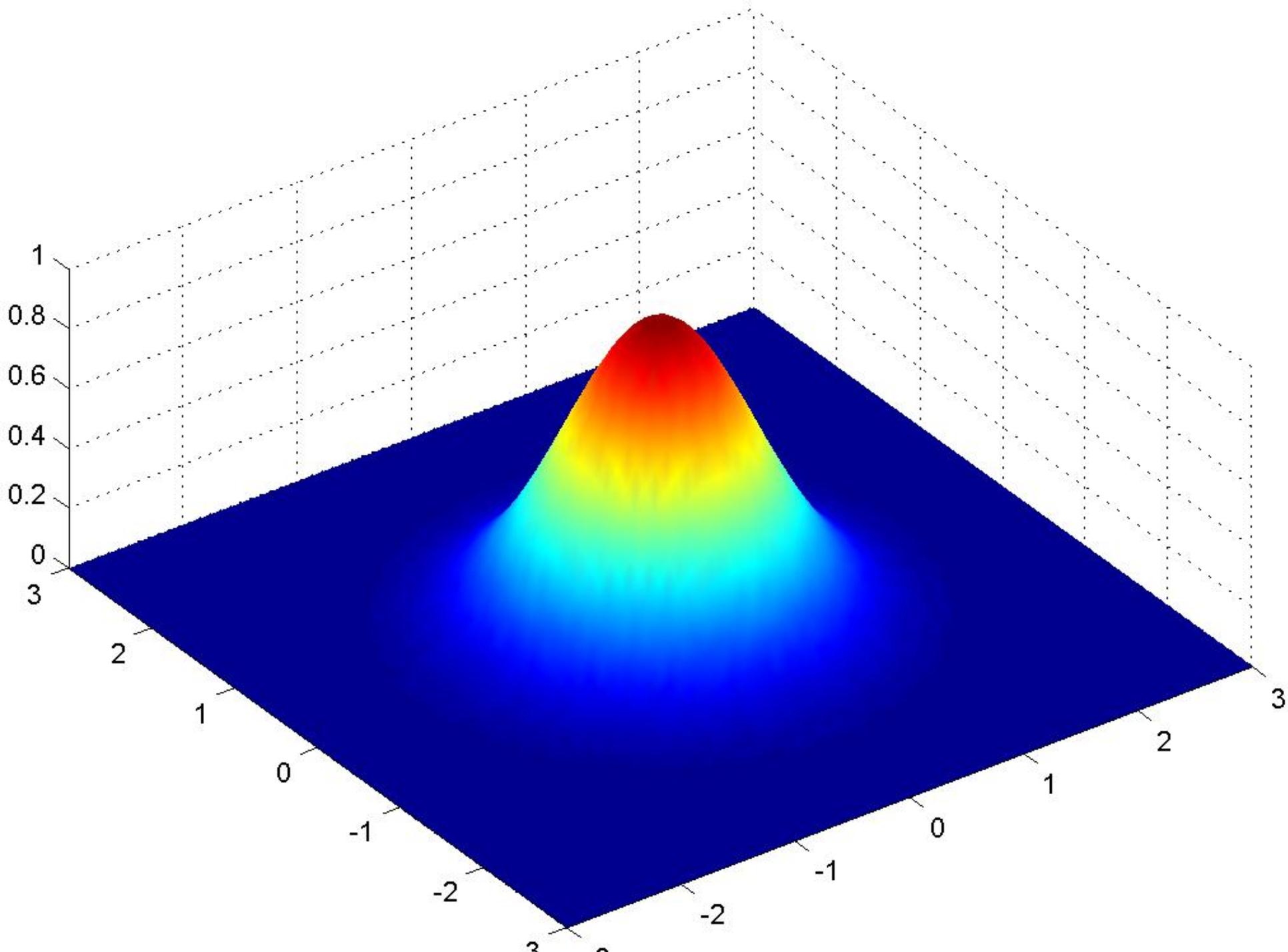
5.50 Myr (Geneva-Bessell)

$\text{Pr}(\tau^2)=0.67$



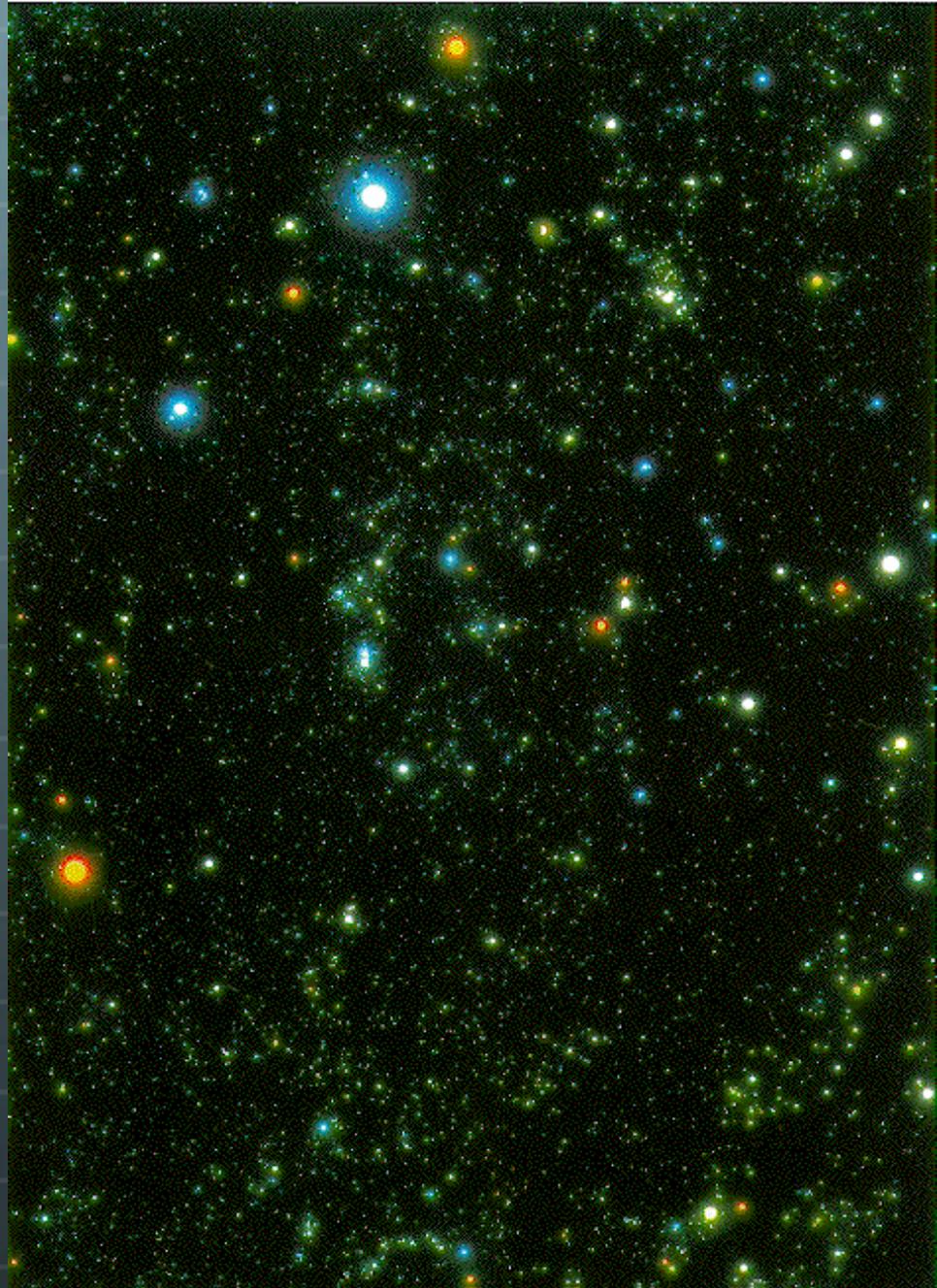
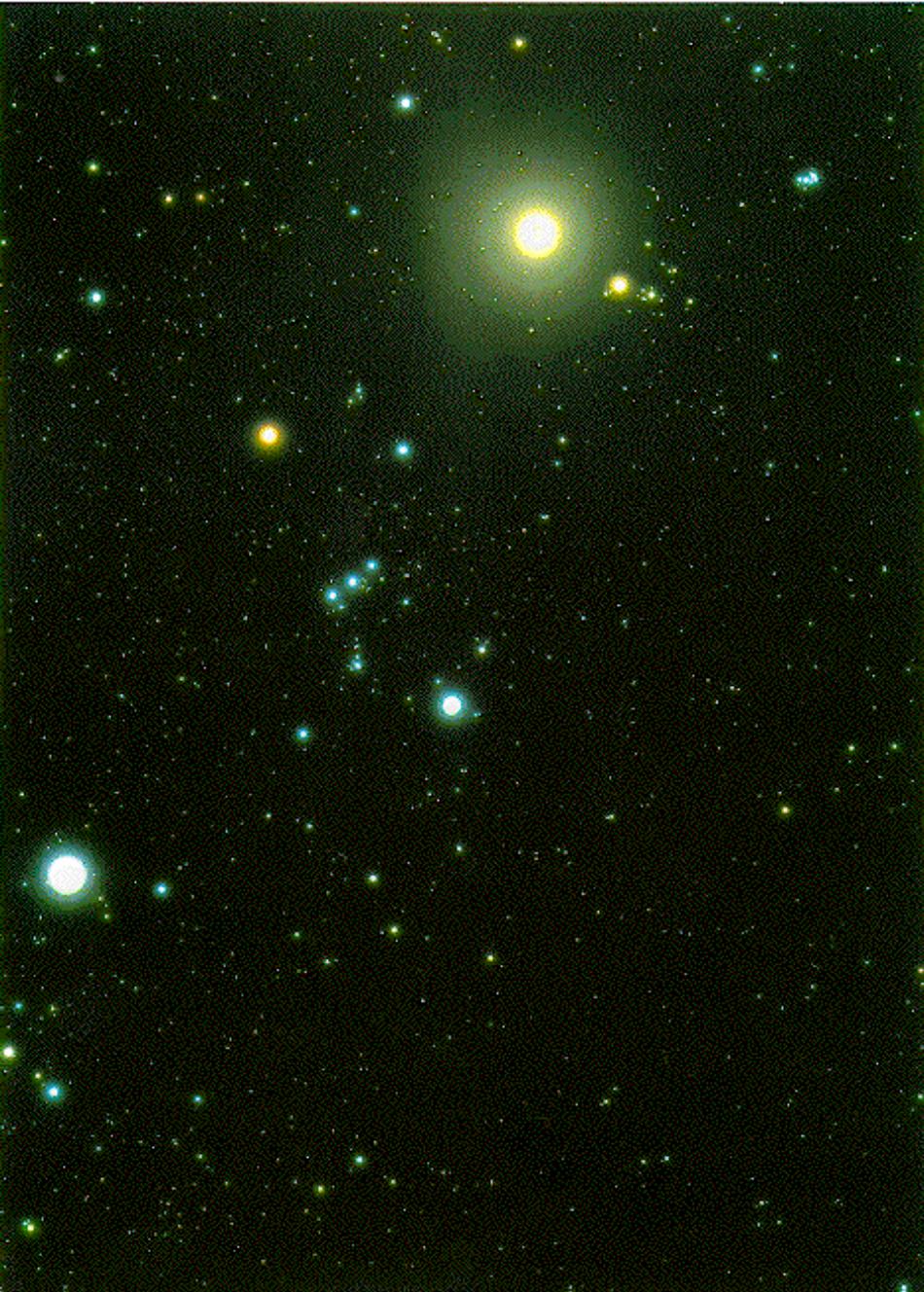


Courtesy NASA/JPL-Caltech.



“There has not been a single date in the history of the law of gravitation when a modern significance test would not have rejected all laws and left us with no law.”

Harold Jeffries, “The theory of probability”, 1939



Leicester X-ray group

The rise of Bayesian methods in astrophysics

